

Finite Element Analysis (FEA) and Thermal Gradient of a Solid Rectangular Fin with Embossing's for Aerospace Applications

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Abstract

Fins are the extended surfaces through which heat transfer takes place by conduction and convection to keep the base surface cool. Fins of various configurations are presently used ranging from automobile engines to cooling of chip in a computer. Fins used presently are solid with different shapes but in the present research such solid fins are compared with solid fins having maximum of 10 numbers of embossing's that further increases the surface area for maximum heat transfer. Importance in this research is given to variation of temperature along the length of the fins which in turn gives rate of heat transfer. Thus this research is under taken to increase the efficiency of fins (by extracting heat from the base surface) which is highly demanded today for air cooled engines, compressors, refrigerators etc. In the present research, SOLID70 element and SURF152 elements are used for FE analysis. Methodology involves 3D rectangular fin modelling and meshing, creation of surf elements for the modeling, applying the boundary conditions and source temperature, applying the material property (aluminum) to obtain the steady state thermal contours. FEA results are finally compared with analytic and experimental values for validity. In the present research, a solid rectangular aluminum fin and the same rectangular fin with 2, 4, 8 and 10 embossing's were compared through finite element analysis for its temperature distribution along the length. FEA analysis of the present research showed that fins having embossing's were more efficient compared to that a simple solid fin. Hence it is concluded from the present research that embossing's at preferred locations further increases the rate of heat transfer. From the present analysis it is concluded that the mathematical and FEA for a solid rectangular fin without embossing's are converging within $\pm 1.2^{\circ}\text{C}$ and rectangular fin with 10 embossing's is converging within $\pm 1.4^{\circ}\text{C}$ and hence the validity.

Keywords

Fin, FEA, Temperature, Embossing and Surface

1. Introduction

The basic law that governs the convective heat transfer is Newton's law of cooling given by:

$$Q = h A (T_s - T_f), \text{ Watts} \quad (1)$$

where: T_s : the surface temperature °C; T_f : the fluid temperature °C; h : the convective heat transfer coefficient $\text{w/m}^2 \text{ }^\circ\text{C}$; A : surface area, m^2 .

Note that in the above equation, film coefficient of heat transfer or the convective heat transfer coefficient " h " is very important which mainly depends on the type of the surface, size, shape, its temperature, surface finish etc. Most of the research, mathematical analysis and dimensional analysis are confined in finding " h ". In addition to the above, for fins, the temperature distribution along its length also becomes important.

The expulsion of overabundance warmth from framework parts is fundamental to abstain from harming impacts of overheating. Thusly the improvement of warmth exchange is a vital subject of warm designing [1]. Heat exchange rate might be expanded by expanding the warmth exchange coefficient between a surface and its encompassing, or by expanding the warmth exchange zone of the surface. Much of the time, the zone of warmth exchange is expanded by developing surfaces. These amplified surfaces are called as fins.

Balances are utilized to improve convective warmth move in an extensive variety of designing applications and offer a handy method for accomplishing a substantial aggregate warmth exchange surface range without the utilization of an over the top measure of essential surface zone [2]. Fins are generally connected for warmth administration in electrical apparatuses, for example, PC power supplies or substation transformers. Different applications incorporate motor cooling, condensers in refrigeration and aerating and cooling [3]. Fins as warmth exchange improvement gadgets have been very regular. The diverse materials like mild steel, stainless steel, aluminum, and silver, copper and so on are utilized for making fins. As the stretched out surface innovation keeps on developing, new outline thoughts have been risen including fins made of anisotropic composites, permeable media, hindered and punctured plates. Because of popularity for light weight, smaller and sparing fins, the enhancement of balance size is of awesome significance [4].

Along these lines, fins must be intended to accomplish most extreme warmth expulsion with least material use considering the simplicity of the balance fabricating. The change in warmth exchange coefficient is ascribed to the restarting of the warm limit layer after every interference [5]. Accordingly punctured plates

and fins speak to a case of surface intrusion. Current study intends to foresee the temperature drop more than a few round apertures of expansion in number. Different parameters like warm flux and warm inclination are analyzed over various number of round holes [6]. In this investigation ANSYS FEA software is utilized for lattice and unraveling.

In the examination of warmth trade, cutting edges are surfaces that stretch out from a thing to manufacture the rate of warmth trade to or from nature by growing convection. The measure of conduction, convection, or radiation of an article chooses the measure of warmth it trades [7]. Extending the temperature incline between the article and the earth, growing the convection heat trade coefficient, or extending the surface zone of the thing constructs the glow trade. Occasionally it is not achievable or down to earth to change the underlying two choices. In this way, adding a cutting edge to a thing assembles the surface zone and can rarely be a calm response for warmth trade issues [8].

Finally, it is well known that major heat transfer from the fin is by convection and performance of a fin is evaluated by its efficiency and effectiveness.

2. Literature Review

There are various examination related to warmth trade and weight drop of channels with pin cutting edges, which are limited to stick parities with round or couple of different cross territories. The genuine warmth trade takes by two modes *i.e.* by conduction took after by convection. Heat trade through the solid to the surface of the solid happens through conduction whereas from the surface to the surroundings happens by convection. Further warmth trade may be by normal convection or by obliged convection.

Bayram Sahin and Alparslan Demir [9] from their research concluded that, the use of the square stick cutting edges may incite warmth trade change. Both lower elbowroom extent and lower between parity scattering extent and likewise cut down Reynolds numbers are proposed for higher warm execution. R. Karthikeyan and R. Rathnasamy [10] concluded from their research that, for a given Reynolds number, the pin-edge show with smaller buries fin separation gives higher execution than those with higher cover equalization partitions. Another researcher found that, most in-line square stick equalization bunches have poorer warmth move than an in-line round pin fin cluster show wonderful warmth trade at high Reynolds number. The perfect between equalization pitches are directed by the greatest Nusselt number at a given pumping power [11]. Connections giving the typical Nusselt number for each outline as a part of the Reynolds number were created few researchers [12]. Amol B., Dhumne, Hemant S. and Farkade [13] focused on the trial examination of on warmth exchange upgrade and the relating weight drop over a level surface equipped with barrel molded cross sectional punctured pin equalizations in a rectangular channel. Their research showed that the usage of the barrel formed punctured pin fins prompts heat trade update than the solid round and empty equalizations. Both

lower breathing space extent and lower between parity scattering extent and nearly cut down Reynolds numbers are proposed for higher warm execution. In one more investigation the researchers found that, glow trade by short stick edges in staggered plans. According to their results, longer stick equalizations ($H/d = 4$) trade more warmth than shorter pin-parities ($H/d = 1/2$ and 2) and the exhibit found the center estimation of warmth trade with eight segments of pin-adjusts to some degree surpasses that with only four lines [14]. Vanfossen G. J. and Brigham B. A. [15] focused their research on the ordinary warmth trade coefficient on the pin surface is around 35% greater than that on the end dividers.

Metzger *et al.*, [16] investigated the effects of pin-edge shape and show presentation on the glow trade and the weight incident in pin-equalization bunches. They demonstrated by their results that the use of round and empty pin-parities with a group introduction amongst astonished and in-line can now and again propel the glow trade, while fundamentally decreasing weight. Others have also reported from their investigation that, another way to deal with upgrade heat swapping scale is touse spaces which allow the stream to encounter the pieces [17]. Yatendra Singh, Tomar, Sahu M. M. [18] mulled over that the warm resistance and weight drop are considered as the distinctive warm execution properties. Their studies have exhibited that the convection heat conversion standard from equalization bunches depends on upon all geometric parameter, parity material and base-to-encompassing temperature contrast. The elliptic pin equalization exhibits the most insignificant weight drops. For the same surface zone at a settled pumping power, the elliptic pin edge has the smallest warm resistance for the stunned course of action [19].

3. Relevance of the Research

Fins are the extended surfaces through which heat transfer takes place by conduction and convection. In the present investigation the surface area is further increased by providing embossing's at preferred locations in the solid fin. This in turn increases effectiveness and efficiency of the fin. So far no attempt has been made to provide embossing's in the solid aluminum fin to increase the surface area and hence the present research was under taken to fill the void.

4. Experimental, Analytical and FE Analysis Procedure

Figure 1 shows the experimental set up showing temperature recorder, thermocouple etc. along with the heat source at the center, attached with fins having embossing's (MAXM. 10). The power supplied was 40 watts to heat the base of the fin.

In the present research, SOLID70 element and SURF152 elements are used for FE analysis. Methodology involves 3D rectangular fin modelling and meshing, creation of surf elements for the modeling, applying the boundary conditions and source temperature, applying the material property (aluminum) to obtain

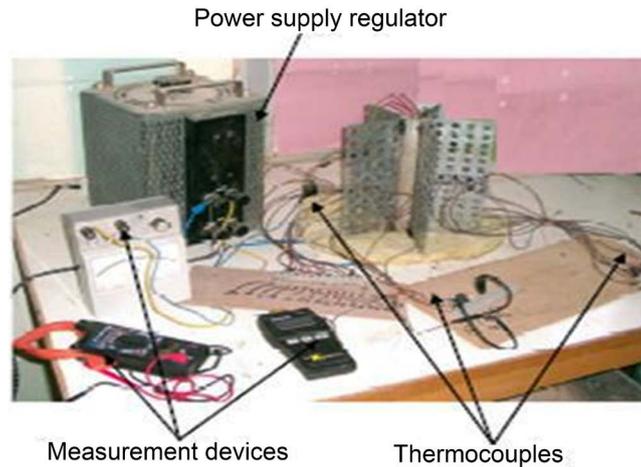


Figure 1. Experimental setup.

the steady state thermal contours. Finally the temperature distribution results of solid fin are compared with that of solid fin with 10 embossing's at preferred locations along the length of the fin.

4.1. Mathematical Analysis For a Solid Fin Temperature Gradient

Figure 2 shows a rectangular aluminum fin indicating the details regarding area, perimeter, temperature etc.

The most popular energy balance equation used to find the heat transfer through fins mathematically (for steady state condition) is given by:

$$Q = \sqrt{hpKA}(C_2 - C_1) \quad (2)$$

where Q : rate of heat transfer, watts, h : convective heat transfer coefficient $w/m^2 \text{ } ^\circ\text{C}$; P : the perimeter of the fin, m, K : thermal conductivity, $w/m \text{ } ^\circ\text{C}$; A : area, m^2 and C_1 ; C_2 are constants obtained by applying the limits.

Above equation is modified to find temperature distribution based on the tip condition.

Equation below is used to find analytically the fin temperature over a distance with given boundary conditions [20].

$$T(X) = T_\infty + (T_b - T_\infty) * \frac{Nr}{Dr} \quad (3)$$

where,

$$Nr = \cosh m(L-x) + \left(\frac{h}{mk}\right) + \sinh m(L-x)$$

$$Dr = \cosh mL + \left(\frac{h}{mk}\right) + \sinh mL$$

4.2. Heat Transfer Coefficient Using Vertical Plate Correlation

Correlations given below are used to find the heat transfer coefficient using dimensional analysis for vertical plate [21].

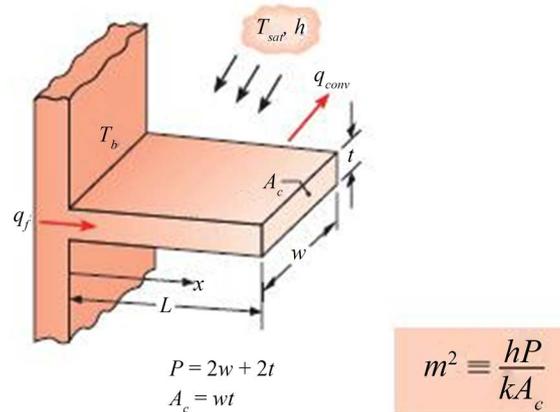


Figure 2. 3D view of rectangular fin.

$$Nu_L = \frac{h * L}{k} = C \left(\frac{g \beta L^3}{\nu \alpha} * (T_s - T_\infty) \right)^n \tag{4}$$

where,

$$h = C * \frac{k}{L} \left(\frac{g \beta L^3}{\nu \alpha} * (T_s - T_\infty) \right)^n = FK \text{constant} * (T_s - T_\infty)^n$$

(where $c = 0.59, n = 0.25$).

4.3. Mathematical and Finite Element Modeling of Rectangular Fin with Number of Embossing's (2, 4, 8 and 10)

For analysis and comparison purpose, rectangular aluminum fin with 2, 4, 8 and 10 embossing's was considered but for discussion only fin with 10 embossing's is presented in the present paper.

Mathematically, the heat transfer coefficient is calculated using the vertical plate correlation using the following correlation.

$$h_{ps} = h * \left(1 + 0.75 * \frac{1130.9}{1696.45} \right) = 2.28 \tag{5}$$

5. Results and Discussions.

5.1. Solid Rectangular Fin without Embossing's

Figure 3 shows FE modeling and analysis for a rectangular fin indicating thermal contour. Temperature along the length of the fin calculated analytically is tabulated in Table 1. Figure 4 shows the superpose of FE analysis and analytical results as indicated in Table 1.

It is observed from Table 1 that the root temperature 200°C goes on decreases as fin length increases and reaches 192.4°C at the tip. From Figure 3 it is again observed that the FE modeling follows the same pattern that the temperature monotonically decreases from 200°C to 192°C. Hence, it is observed from the present research that keeping the base (root) temperature at 200°C with power

Table 1. Tabulation of analytic values of temperature along the length of the fin.

Analytic calculation to find temperature at distance x					
L , Length of the fin					0.15 m
w , width of the fin					0.1 m
t , thickness of the fin					0.015 m
h , heat transfer coeff.					5.489 w/m ² -k (for Al)
p , perimeter					0.23 m
A_c , cross section Area					0.0015 m ²
k , thermal conductivity					236 w/m-k (for Al)
m					1.888
T base					200°C
T infinity					20°C

L (inm)	X (in m)	Numerator	Denominator	Theta (a)/theta (b)	T(x), °C
0.15	0	1.0439	1.0439	1.0000	200.0
	0.015	1.0358	1.0439	0.9923	198.6
	0.03	1.0286	1.0439	0.9823	197.4
	0.045	1.0222	1.0439	0.9792	196.3
	0.06	1.0166	1.0439	0.9738	195.3
	0.075	1.0118	1.0439	0.9692	194.5
	0.09	1.0078	1.0439	0.9654	193.8
	0.105	1.0047	1.0439	0.9624	193.2
	0.12	1.0023	1.0439	0.9601	192.8
	0.135	1.0008	1.0439	0.9586	192.6
	0.15	1.0000	1.0439	0.9579	192.4

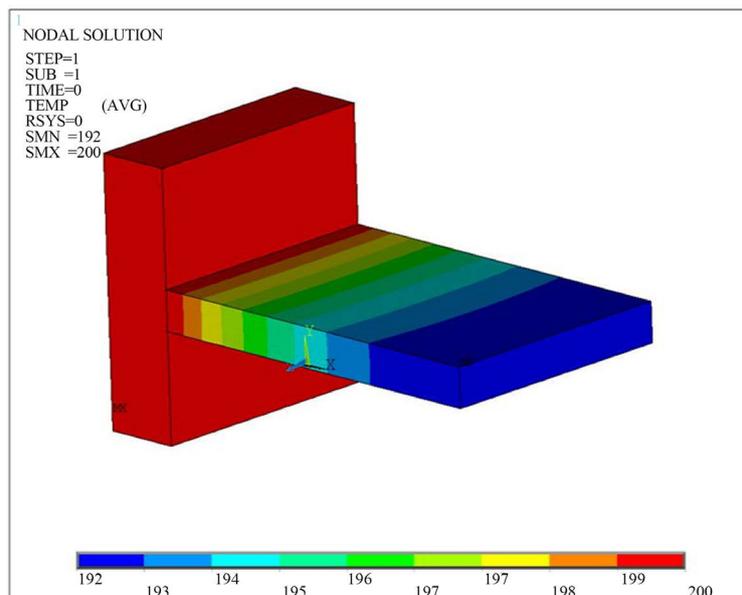


Figure 3. Thermal contour (FE analysis).

Temperature vs Distance

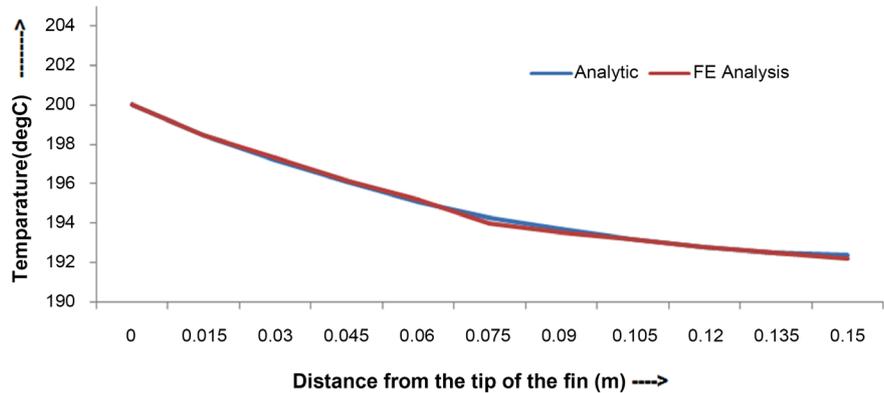


Figure 4. Variation of temperature along the fin length (analytical and FEA superposed).

supply of 40 watts, a solid rectangular fin reaches a temperature of 192.4°C at the tip. From **Figure 4** it is observed that the mathematical and FEA that for a solid rectangular fin without embossing's are converging within $\pm 1.2^\circ\text{C}$ and hence the validity of FEA with mathematical analysis.

5.2. Solid Rectangular Fin with Embossing's

Figure 5 shows the experimental results of temperature measurements along the length of the fin with a power supply of 40 watts for a rectangular fin with 2, 4, 8 and 10 embossing's. Temperature was measured using thermocouples along the length of the fin.

Figure 6 shows the temperature calculated using mathematical analysis for a rectangular fin containing 2, 4, 8 and 10 embossing's.

Figures 7-10 show the FE modelling for geometry, meshing, steady state thermal contour and heat flux for a rectangular fin containing 10 embossing's.

It is observed from **Figure 5** and **Figure 6** that both experimental and mathematical analysis follows almost the same pattern of temperature distribution along the length of the embossed fin. It is also observed from **Figure 5** and **Figure 6** that the temperature of fin at the trailing surface is decreasing with increase the number of embossing's in the fin. This indicates that heat transfer increases with embossing's having full connectivity between the base and the fin. It is observed from the present research that keeping the base (root) temperature at 200°C with power supply of 40 watts, rectangular fin with 10 embossing's reaches 179°C at the tip (**Figure 9**). This shows that rectangular fin with embossing's removes more heat compared to solid fin.

From **Figure 9** it is observed that FE analysis follows the same pattern as that of mathematical and experimental values (calculations not shown) *i.e.*, the root temperature 200°C continuously decreases to 179°C at the tip.

It is finally observed that the mathematical and FEA of rectangular fin with 10

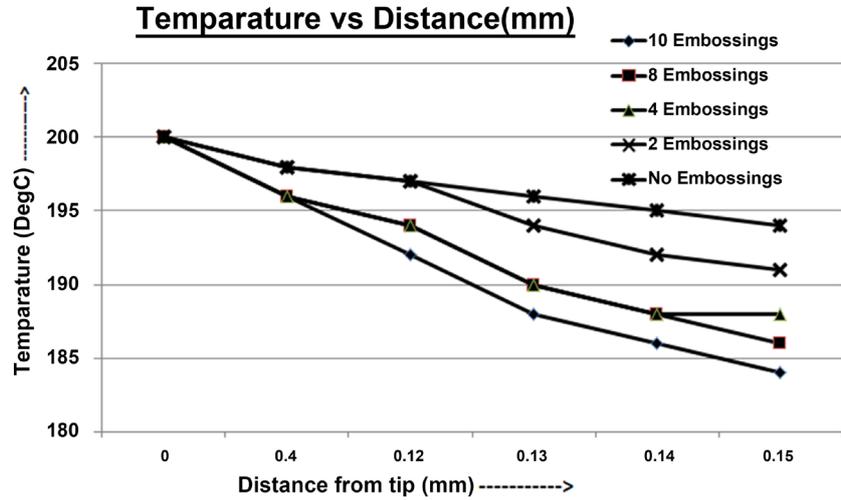


Figure 5. Plot of temperature vs length for a rectangular fin with embossing's.

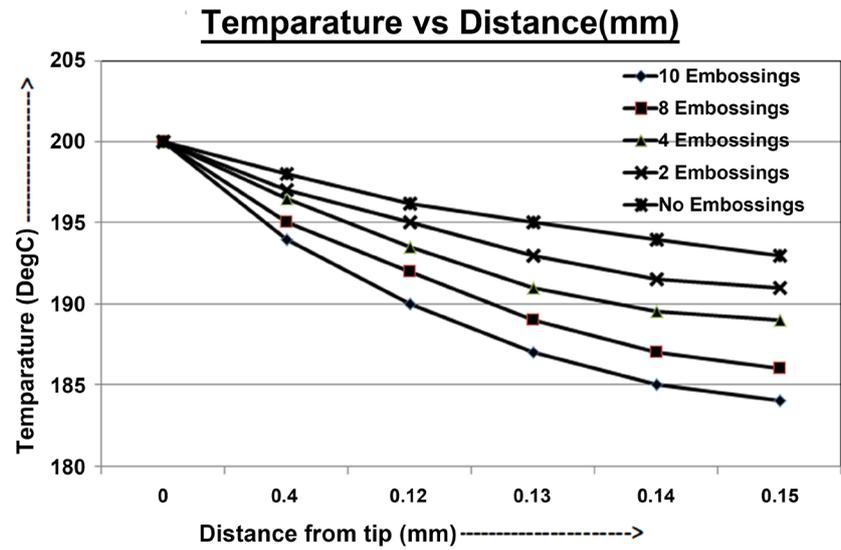


Figure 6. Plot showing temperature vs distance for a rectangular fin with 2, 4, 8 and 10 embossing's by mathematical analysis.

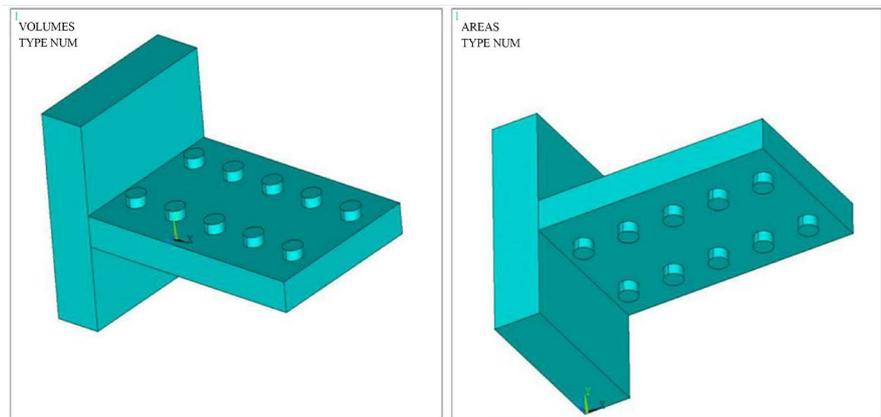


Figure 7. Geometry of fin with 10 embossing's.

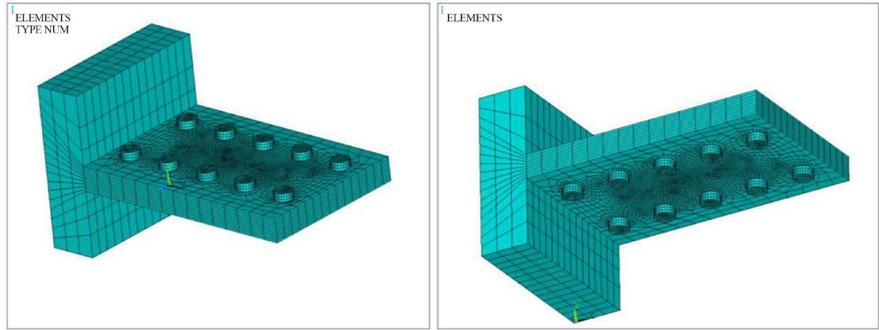


Figure 8. Finite element model (meshing) of the fin with embossing's.

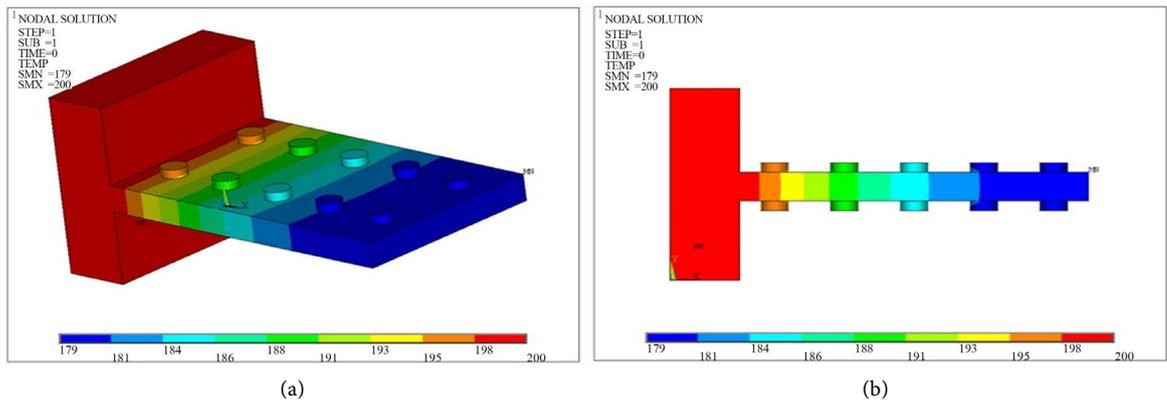


Figure 9. Steady state thermal contour of embossed fin. (a) Max temperature = 200°C; (b) Min temperature = 179°C.

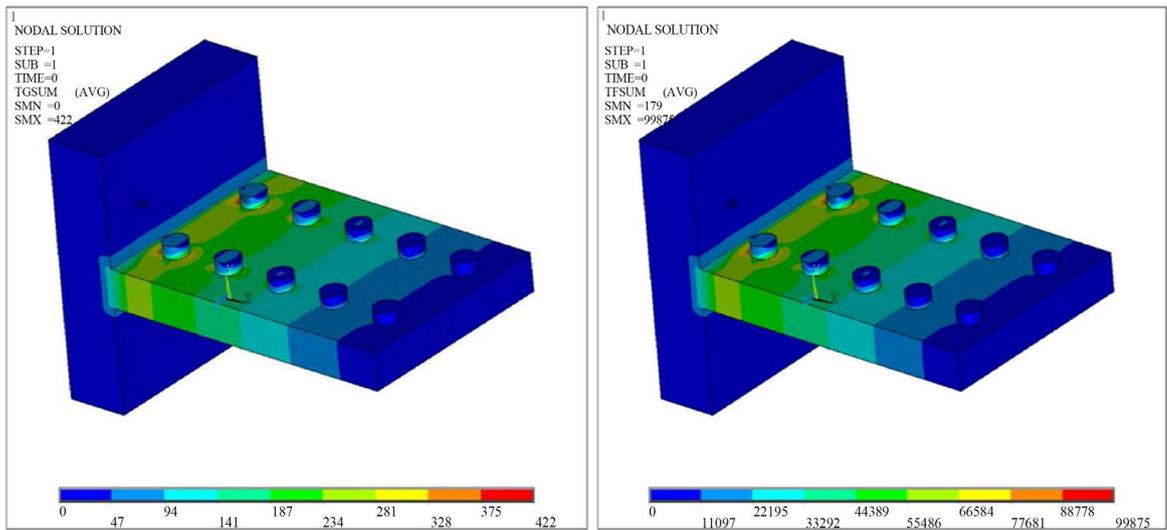


Figure 10. Contours of thermal gradient and heat flux of embossed fin.

embossing's are converging within $\pm 1.4^\circ\text{C}$ and hence the validity of FEA with mathematical and experimental analysis.

6. Conclusions

It is observed from the present research that keeping the base (root) temperature

at 200°C with power supply of 40 watts, a solid rectangular fin reaches a temperature of 192°C at the tip whereas the same fin with 10 embossing's reaches 179°C at the tip. This shows that rectangular fin with embossing's removes more heat compared to that of a solid fin. It is also observed from the research that this temperature fall is gradual from fin with 2, 4, 8 and 10 embossing's. Thus the heat removal gradually decreases with increase in embossing's. Heat flux also follows the same pattern along the length of the fin as that of the temperature.

In the present research it is also observed from the mathematical and FEA that a solid rectangular fin without embossing's is converging within $\pm 1.2^\circ\text{C}$ and rectangular fin with 10 embossing's is converging within $\pm 1.4^\circ\text{C}$ and hence the validity.

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